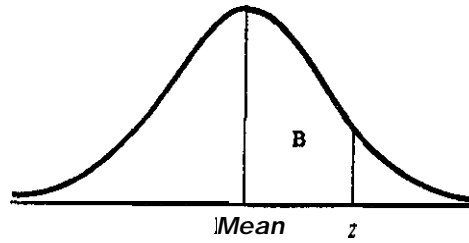




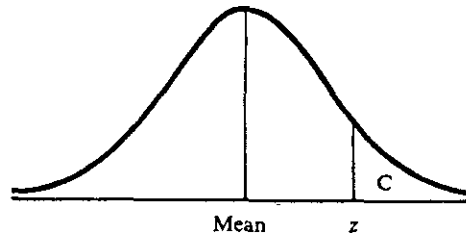
**Table A Areas Under the Normal Curve**

Column A gives the positive  $z$  score.

Column B gives the area between the mean and  $z$ . Since the curve is symmetrical, areas for negative  $z$  scores are the same as for positive ones.



Column C gives the area that is beyond  $z$ .



| $z$<br>A | Area<br>between<br>mean and $z$<br>B | Area<br>beyond<br>$z$<br>C | $z$<br>A | Area<br>between<br>mean and $z$<br>B | Area<br>beyond<br>$z$<br>C |
|----------|--------------------------------------|----------------------------|----------|--------------------------------------|----------------------------|
| 0.00     | .0000                                | .5000                      | 0.25     | .0987                                | .4013                      |
| 0.01     | .0040                                | .4960                      | 0.26     | .1026                                | .3974                      |
| 0.02     | .0080                                | .4920                      | 0.27     | .1064                                | .3936                      |
| 0.03     | .0120                                | .4880                      | 0.28     | .1103                                | .3897                      |
| 0.04     | .0160                                | .4840                      | 0.29     | .1141                                | .3859                      |
| 0.05     | .0199                                | .4801                      | 0.30     | .1179                                | .3821                      |
| 0.06     | .0239                                | .4761                      | 0.31     | .1217                                | .3783                      |
| 0.07     | .0279                                | .4721                      | 0.32     | .1255                                | .3745                      |
| 0.08     | .0319                                | .4681                      | 0.33     | .1293                                | .3707                      |
| 0.09     | .0359                                | .4641                      | 0.34     | .1331                                | .3669                      |
| 0.10     | .0398                                | .4602                      | 0.35     | .1368                                | .3632                      |
| 0.11     | .0438                                | .4562                      | 0.36     | .1406                                | .3594                      |
| 0.12     | .0478                                | .4522                      | 0.37     | .1443                                | .3557                      |
| 0.13     | .0517                                | .4483                      | 0.38     | .1480                                | .3520                      |
| 0.14     | .0557                                | .4443                      | 0.39     | .1517                                | .3483                      |
| 0.15     | .0596                                | .4404                      | 0.40     | .1554                                | .3446                      |
| 0.16     | .0636                                | .4364                      | 0.41     | .1591                                | .3409                      |
| 0.17     | .0675                                | .4325                      | 0.42     | .1628                                | .3372                      |
| 0.18     | .0714                                | .4286                      | 0.43     | .1664                                | .3336                      |
| 0.19     | .0753                                | .4247                      | 0.44     | .1700                                | .3300                      |
| 0.20     | .0793                                | .4207                      | 0.45     | .1736                                | .3264                      |
| 0.21     | .0832                                | .4168                      | 0.46     | .1772                                | .3228                      |
| 0.22     | .0871                                | .4129                      | 0.47     | .1808                                | .3192                      |
| 0.23     | .0910                                | .4090                      | 0.48     | .1844                                | .3156                      |
| 0.24     | .0948                                | .4052                      | 0.49     | .1879                                | .3121                      |

**Table A (Continued)**

| <i>z</i> | <i>Area<br/>between<br/>mean and z</i> | <i>Area<br/>beyond<br/>z</i> | <i>z</i> | <i>Area<br/>between<br/>mean and z</i> | <i>Area<br/>beyond<br/>z</i> |
|----------|--|------------------------------|----------|--|------------------------------|
| A        | B                                      | C                            | A        | B                                      | C                            |
| 0.50     | .1915                                  | .3085                        | 0.95     | .3289                                  | .1711                        |
| 0.51     | .1950                                  | .3050                        | 0.96     | .315                                   | .1685                        |
| 0.52     | .1985                                  | .3015 ✓                      | 0.97     | .3340                                  | .1660                        |
| 0.53     | .2019                                  | .2981                        | 0.98     | .3365                                  | .1635                        |
| 0.54     | .2054                                  | .2946                        | 0.99     | .3389                                  | .1611                        |
| 0.55     | .2088                                  | .2912                        | 1.00     | .3413                                  | .1587                        |
| 0.56     | .2123                                  | .2877                        | 1.01     | .3438                                  | .1562                        |
| 0.57     | .2157                                  | .2843                        | 1.02     | .3461                                  | .1539                        |
| 0.58     | .2190                                  | .2810                        | 1.03     | .3485                                  | .1515                        |
| 0.59     | .2224                                  | .2776                        | 1.04     | .3508                                  | .1492                        |
| 0.60     | .2257                                  | .2743                        | 1.05     | .3531                                  | .1469                        |
| 0.61     | .2291                                  | .2709                        | 1.06     | .3554                                  | .1446                        |
| 0.62     | .2324                                  | .2676                        | 1.07     | .3577                                  | .1423                        |
| 0.63     | .2357                                  | .2643                        | 1.08     | .3599                                  | .1401                        |
| 0.64     | .2389                                  | .2611                        | 1.09     | .3621                                  | .1379                        |
| 0.65     | .2422                                  | .2578                        | 1.10     | .3643                                  | .1357                        |
| 0.66     | .2454                                  | .2546                        | 1.11     | .3665                                  | .1335                        |
| 0.67     | .2486                                  | .2514                        | 1.12     | .3686                                  | .1314                        |
| 0.68     | .2517                                  | .2483                        | 1.13     | .3708                                  | .1292                        |
| 0.69     | .2549                                  | .2451                        | 1.14     | .3729                                  | .1271                        |
| 0.70     | .2580                                  | .2420                        | 1.15     | .3749                                  | .1251                        |
| 0.71     | .2611                                  | .2389                        | 1.16     | .3770                                  | .1230                        |
| 0.72     | .2642                                  | .2358                        | 1.17     | .3790                                  | .1210                        |
| 0.73     | .2673                                  | .2327                        | 1.18     | .3810                                  | .1190                        |
| 0.74     | .2704                                  | .2296                        | 1.19     | .3830                                  | .1170                        |
| 0.75     | .2734                                  | .2266                        | 1.20     | .3849                                  | .1151                        |
| 0.76     | .2764                                  | .2236                        | 1.21     | .3869                                  | .1131                        |
| 0.77     | .2794                                  | .2206                        | 1.22     | .3888                                  | .1112                        |
| 0.78     | .2823                                  | .2177                        | 1.23     | .3907                                  | .1093                        |
| 0.79     | .2852                                  | .2148                        | 1.24     | .3925                                  | .1075                        |
| 0.80     | .2881                                  | .2119                        | 1.25     | .3944                                  | .1056                        |
| 0.81     | .2910                                  | .2090                        | 1.26     | .3962                                  | .1038                        |
| 0.82     | .2939                                  | .2061                        | 1.27     | .3980                                  | .1020                        |
| 0.83     | .2967                                  | .2033                        | 1.28     | .3997                                  | .1003                        |
| 0.84     | .2995                                  | .2005                        | 1.29     | .4015                                  | .0985                        |
| 0.85     | .3023                                  | .1977                        | 1.30     | .4032                                  | .0968                        |
| 0.86     | .3051                                  | .1949                        | 1.31     | .4049                                  | .0951                        |
| 0.87     | .3078                                  | .1922                        | 1.32     | .4066                                  | .0934                        |
| 0.88     | .3106                                  | .1894                        | 1.33     | .4082                                  | .0918                        |
| 0.89     | .3133                                  | .1867                        | 1.34     | .4099                                  | .0901                        |
| 0.90     | .3159                                  | .1841                        | 1.35     | .4115                                  | .0885                        |
| 0.91     | .3186                                  | .1814                        | 1.36     | .4131                                  | .0869                        |
| 0.92     | .3212                                  | .1788                        | 1.37     | .4147                                  | .0853                        |
| 0.93     | .3238                                  | .1762                        | 1.38     | .4162                                  | .0838                        |
| 0.94     | .3264                                  | .1736                        | 1.39     | .4177                                  | .0823                        |

**Table A (Continued)**

| <i>z</i> | <i>Area between mean and z</i> |          | <i>z</i> | <i>Area between mean and z</i> |          |
|----------|--------------------------------|----------|----------|--------------------------------|----------|
|          | <i>B</i>                       | <i>C</i> |          | <i>A</i>                       | <i>B</i> |
| 1.40     | .4192                          | .0808    | 1.85     | .4678                          | .0322    |
| 1.41     | .4207                          | .0793    | 1.86     | .4686                          | .0314    |
| 1.42     | .4222                          | .0778    | 1.87     | .4693                          | .0307    |
| 1.43     | .4236                          | .0764    | 1.88     | .4699                          | .0301    |
| 1.44     | .4251                          | .0749    | 1.89     | .4706                          | .0294    |
| 1.45     | .4265                          | .0735    | 1.90     | .4713                          | .0287    |
| 1.46     | .4279                          | .0721    | 1.91     | .4719                          | .0281    |
| 1.47     | .4292                          | .0708    | 1.92     | .4726                          | .0274    |
| 1.48     | .4306                          | .0694    | 1.93     | .4732                          | .0268    |
| 1.49     | .4319                          | .0681    | 1.94     | .4738                          | .0262    |
| 1.50     | .4332                          | .0668    | 1.95     | .4744                          | .0256    |
| 1.51     | .4345                          | .0655    | 1.96     | .4750                          | .0250    |
| 1.52     | .4357                          | .0643    | 1.97     | .4756                          | .0244    |
| 1.53     | .4370                          | .0630    | 1.98     | .4761                          | .0239    |
| 1.54     | .4382                          | .0618    | 1.99     | .4767                          | .0233    |
| 1.55     | .4394                          | .0606    | 2.00     | .4772                          | .0228    |
| 1.56     | .4406                          | .0594    | 2.01     | .4778                          | .0222    |
| 1.57     | .4418                          | .0582    | 2.02     | .4783                          | .0217    |
| 1.58     | .4429                          | .0571    | 2.03     | .4788                          | .0212    |
| 1.59     | .4441                          | .0559    | 2.04     | .4793                          | .0207    |
| 1.60     | .4452                          | .0548    | 2.05     | .4798                          | .0202    |
| 1.61     | .4463                          | .0537    | 2.06     | .4803                          | .0197    |
| 1.62     | .4474                          | .0526    | 2.07     | .4808                          | .0192    |
| 1.63     | .4484                          | .0516    | 2.08     | .4812                          | .0188    |
| 1.64     | .4495                          | .0505 ✓  | 2.09     | .4817                          | .0183    |
| 1.65     | .4505                          | .0495 ✓  | 2.10     | .4821                          | .0179    |
| 1.66     | .4515                          | .0485    | 2.11     | .4826                          | .0174    |
| 1.67     | .4525                          | .0475    | 2.12     | .4830                          | .0170    |
| 1.68     | .4535                          | .0465    | 2.13     | .4834                          | .0166    |
| 1.69     | .4545                          | .0455    | 2.14     | .4838                          | .0162    |
| 1.70     | .4554                          | .0446    | 2.15     | .4842                          | .0158    |
| 1.71     | .4564                          | .0436    | 2.16     | .4846                          | .0154    |
| 1.72     | .4573                          | .0427    | 2.17     | .4850                          | .0150    |
| 1.73     | .4582                          | .0418    | 2.18     | .4854                          | .0146    |
| 1.74     | .4591                          | .0409    | 2.19     | .4857                          | .0143    |
| 1.75     | .4599                          | .0401    | 2.20     | .4861                          | .0139    |
| 1.76     | .4608                          | .0392    | 2.21     | .4864                          | .0136    |
| 1.77     | .4616                          | .0384    | 2.22     | .4868                          | .0132    |
| 1.78     | .4625                          | .0375    | 2.23     | .4871                          | .0129    |
| 1.79     | .4633                          | .0367    | 2.24     | .4875                          | .0125    |
| 1.80     | .4641                          | .0359    | 2.25     | .4878                          | .0122    |
| 1.81     | .4649                          | .0351    | 2.26     | .4881                          | .0119    |
| 1.82     | .4656                          | .0344    | 2.27     | .4884                          | .0116    |
| 1.83     | .4664                          | .0336    | 2.28     | .4887                          | .0113    |
| 1.84     | .4671                          | .0329    | 2.29     | .4890                          | .0110    |

**Table A (Continued)**

| <i>z</i> | <i>Area<br/>between<br/>mean and z</i> | <i>Area<br/>beyond<br/>z</i> | <i>z</i> | <i>Area<br/>between<br/>mean and z</i> | <i>Area<br/>beyond<br/>z</i> |
|----------|--|------------------------------|----------|--|------------------------------|
| <i>A</i> | <i>B</i>                               | <i>C</i>                     | <i>A</i> | <i>B</i>                               | <i>C</i>                     |
| 2.30     | .4893                                  | .0107                        | 2.70     | .4965                                  | .0035                        |
| 2.31     | .4896                                  | .0104                        | 2.71     | .4966                                  | .0034                        |
| 2.32     | .4898                                  | .0102                        | 2.72     | .4967                                  | .0033                        |
| 2.33     | .4901                                  | .0099                        | 2.73     | .4968                                  | .0032                        |
| 2.34     | .4904                                  | .0096                        | 2.74     | .4969                                  | .0031                        |
| 2.35     | .4906                                  | .0094                        | 2.75     | .4970                                  | .0030                        |
| 2.36     | .4909                                  | .0091                        | 2.76     | .4971                                  | .0029                        |
| 2.37     | .4911                                  | .0089                        | 2.77     | .4972                                  | .0028                        |
| 2.38     | .4913                                  | .0087                        | 2.78     | .4973                                  | .0027                        |
| 2.39     | .4916                                  | .0084                        | 2.79     | .4974                                  | .0026                        |
| 2.40     | .4918                                  | .0082                        | 2.80     | .4974                                  | .0026                        |
| 2.41     | .4920                                  | .0080                        | 2.81     | .4975                                  | .0025                        |
| 2.42     | .4922                                  | .0078                        | 2.82     | .4976                                  | .0024                        |
| 2.43     | .4925                                  | .0075                        | 2.83     | .4977                                  | .0023                        |
| 2.44     | .4927                                  | .0073                        | 2.84     | .4977                                  | .0023                        |
| 2.45     | .4929                                  | .0071                        | 2.85     | .4978                                  | .0022                        |
| 2.46     | .4931                                  | .0069                        | 2.86     | .4979                                  | .0021                        |
| 2.47     | .4932                                  | .0068                        | 2.87     | .4979                                  | .0021                        |
| 2.48     | .4934                                  | .0066                        | 2.88     | .4980                                  | .0020                        |
| 2.49     | .4936                                  | .0064                        | 2.89     | .4981                                  | .0019                        |
| 2.50     | .4938                                  | .0062                        | 2.90     | .4981                                  | .0019                        |
| 2.51     | .4940                                  | .0060                        | 2.91     | .4982                                  | .0018                        |
| 2.52     | .4941                                  | .0059                        | 2.92     | .4982                                  | .0018                        |
| 2.53     | .4943                                  | .0057                        | 2.93     | .4983                                  | .0017                        |
| 2.54     | .4945                                  | .0055                        | 2.94     | .4984                                  | .0016                        |
| 2.55     | .4946                                  | .0054                        | 2.95     | .4984                                  | .0016                        |
| 2.56     | .4948                                  | .0052                        | 2.96     | .4985                                  | .0015                        |
| 2.57     | .4949                                  | .0051                        | 2.97     | .4985                                  | .0015                        |
| 2.58     | .4951                                  | .0049                        | 2.98     | .4986                                  | .0014                        |
| 2.59     | .4952                                  | .0048                        | 2.99     | .4986                                  | .0014                        |
| 2.60     | .4953                                  | .0047                        | 3.00     | .4987                                  | .0013                        |
| 2.61     | .4955                                  | .0045                        | 3.01     | .4987                                  | .0013                        |
| 2.62     | .4956                                  | .0044                        | 3.02     | .4987                                  | .0013                        |
| 2.63     | .4957                                  | .0043                        | 3.03     | .4988                                  | .0012                        |
| 2.64     | .4959                                  | .0041                        | 3.04     | .4988                                  | .0012                        |
| 2.65     | .4960                                  | .0040                        | 3.05     | .4989                                  | .0011                        |
| 2.66     | .4961                                  | .0039                        | 3.06     | .4989                                  | .0011                        |
| 2.67     | .4962                                  | .0038                        | 3.07     | .4989                                  | .0011                        |
| 2.68     | .4963                                  | .0037                        | 3.08     | .4990                                  | .0010                        |
| 2.69     | .4964                                  | .0036                        | 3.09     | .4990                                  | .0010                        |

**Table A (Continued)**

| <i>z</i> | <i>Area<br/>between<br/>mean and z</i> | <i>Area<br/>beyond<br/>z</i> | <i>z</i> | <i>Area<br/>between<br/>mean and z</i> | <i>Area<br/>beyond<br/>z</i> |
|----------|--|------------------------------|----------|--|------------------------------|
| <i>A</i> | <i>B</i>                               | <i>C</i>                     | <i>A</i> | <i>B</i>                               | <i>C</i>                     |
| 3.10     | .4990                                  | .0010                        | 3.20     | .4993                                  | .0007                        |
| 3.11     | .4991                                  | .0009                        | 3.21     | .4993                                  | .0007                        |
| 3.12     | .4991                                  | .0009                        | 3.22     | .4994                                  | .0006                        |
| 3.13     | .4991                                  | .0009                        | 3.23     | .4994                                  | .0006                        |
| 3.14     | .4992                                  | .0008                        | 3.24     | .4994                                  | .0006                        |
| 3.15     | .4992                                  | .0008                        | 3.30     | .4995                                  | .0005                        |
| 3.16     | .4992                                  | .0008                        | 3.40     | .4997                                  | .0003                        |
| 3.17     | .4992                                  | .0008                        | 3.50     | .4998                                  | .0002                        |
| 3.18     | .4993                                  | .0007                        | 3.60     | .4998                                  | .0002                        |
| 3.19     | .4993                                  | .0007                        | 3.70     | .4999                                  | .0001                        |

**Table B** Critical Values of Student's *t* Distribution

The values listed in the table are the critical values of *t* for the specified degrees of freedom (left column) and the alpha level (column heading). For two-tailed alpha levels,  $t_{crit}$  is both + and -. To be significant,  $|t_{obs}| \geq |t_{crit}|$ .

| df = (n - 1) <i>df</i> | Level of Significance for One-Tailed Test   |         |         |              |         |         |
|------------------------|---|---------|---------|--------------|---------|---------|
|                        | .10   | .05     | .025    | .01          | .005    | .0005   |
|                        | Level of Significance for Two-Tailed Test ✓ |         |         |              |         |         |
|                        | .20   | .10     | .05     | .02          | .01     | .001    |
| 1                      | 3.078                                       | 6.314   | 12.706  | 31.821       | 63.657  | 636.617 |
| 2                      | 1.886                                       | 2.920   | 4.303   | 6.965        | 9.925   | 31.598  |
| 3                      | 1.638                                       | 2.353   | 3.182   | 4.541        | 5.841   | 12.941  |
| 4                      | 1.533                                       | 2.132   | 2.776   | 3.747        | 4.604   | 8.610   |
| 5                      | 1.476                                       | 2.015   | 2.571 ✓ | 3.365        | 4.032   | 6.859   |
| 6                      | 1.440 ✓                                     | 1.943   | 2.447   | 3.143 ✓      | 3.707   | 5.959   |
| 7                      | 1.415                                       | 1.895   | 2.365   | 2.998        | 3.499   | 5.405   |
| 8                      | 1.397                                       | 1.860   | 2.306   | 2.896        | 3.355   | 5.041   |
| 9                      | 1.383                                       | 1.833   | 2.262   | <u>2.821</u> | 3.250   | 4.781   |
| 10                     | 1.372                                       | 1.812   | 2.228   | 2.764        | 3.169   | 4.587   |
| 11                     | 1.363                                       | 1.796   | 2.201   | 2.718        | 3.106   | 4.437   |
| 12                     | 1.356                                       | 1.782   | 2.179   | 2.681        | 3.055   | 4.318   |
| 13                     | 1.350                                       | 1.771   | 2.160   | 2.650        | 3.012   | 4.221   |
| ✓ 14                   | 1.345                                       | 1.761   | 2.145 ✗ | 2.624        | 2.977   | 4.140   |
| 15                     | 1.341                                       | 1.753   | 2.131,  | 2.602        | 2.947   | 4.073   |
| 16                     | 1.337                                       | 1.746   | 2.120   | 2.583        | 2.921   | 4.015   |
| 17                     | 1.333                                       | 1.740   | 2.110   | 2.567        | 2.898   | 3.965   |
| ✓ 18                   | 1.330                                       | 1.734   | 2.101   | 2.552        | 2.878   | 3.922   |
| 19                     | 1.328                                       | 1.729 ✓ | 2.093   | 2.539        | 2.861   | 3.883   |
| 20                     | 1.325                                       | 1.725   | 2.086 ✓ | 2.528        | 2.845   | 3.850   |
| 21                     | 1.323                                       | 1.721   | 2.080   | 2.518        | 2.831 ✓ | 3.819   |
| 22                     | 1.321                                       | 1.717   | 2.074   | 2.508        | 2.819   | 3.792   |
| 23                     | 1.319                                       | 1.714   | 2.069   | 2.500        | 2.807   | 3.767   |
| 24                     | 1.318                                       | 1.711   | 2.064   | 2.492        | 2.797   | 3.745   |
| 25                     | 1.316                                       | 1.708   | 2.060   | 2.485        | 2.787   | 3.725   |
| 26                     | 1.315                                       | 1.706   | 2.056   | 2.479        | 2.779   | 3.707   |
| 27                     | 1.314                                       | 1.703   | 2.052   | 2.473        | 2.771   | 3.690   |
| 28                     | 1.313                                       | 1.701   | 2.048   | 2.467        | 2.763   | 3.674   |
| 29                     | 1.311                                       | 1.699   | 2.045   | 2.462        | 2.756   | 3.659   |
| 30                     | 1.310                                       | 1.697   | 2.042   | 2.457        | 2.750   | 3.646   |
| 40                     | 1.303                                       | 1.684   | 2.021   | 2.423        | 2.704   | 3.551   |
| 60                     | 1.296                                       | 1.671   | 2.000   | 2.390        | 2.660   | 3.460   |
| 120                    | 1.289                                       | 1.658   | 1.980   | 2.358        | 2.617   | 3.373   |
| ∞                      | 1.282                                       | 1.645   | 1.960   | 2.326        | 2.576   | 3.291   |

Table C

**REJECTION REGIONS (z)****Level of Significance**

| Test                        | $\alpha = .01$                        | $\alpha = .05$                        | $\alpha = .10$                        |
|-----------------------------|---------------------------------------|---------------------------------------|---------------------------------------|
| <b>2-Tailed</b>             | $z \leq -2.58$<br>or<br>$z \geq 2.58$ | $z \leq -1.96$<br>or<br>$z \geq 1.96$ | $z \leq -1.65$<br>or<br>$z \geq 1.65$ |
| <b>1-Tailed<br/>(upper)</b> | $z \geq 2.33$                         | $z \geq 1.65$                         | $z \geq 1.28$                         |
| <b>1-Tailed<br/>(lower)</b> | $z \leq -2.33$                        | $z \leq -1.65$                        | $z \leq -1.28$                        |



TABLE D  
CHOOSING AMONG STATISTICAL TECHNIQUES

| Major research question                       | Number of dependent variables  | Number of independent variables     | Covariates                 | Analytic technique  | Goal of analysis   |
|---|--------------------------------|-------------------------------------|----------------------------|---|--|
| Degree of relationship among variables        | One                            | One                                 | None                       | Bivariate r   | Create a linear combination of IVs to optimally predict DV                     |
|   |                                | Multiple                            | None                       | Multiple R  |  |
|   | Multiple                       | Multiple                            | None                       | Hierarchical Multiple R   |  |
|   |                                |                                     | Some                       | Multiple R  |  |
|   | None                           | Multiple (discrete)                 | None                       | Canonical R   |  |
| One (discrete)                                | Multiple (discrete)            | None                                | Multway frequency analysis | Create a loglinear combination of IVs to optimally predict category frequencies |  |
| Significance of group differences             | One                            | One                                 | None                       | One-way ANOVA or t-test   | Create a linear combination of DVs to maximize group differences               |
|   |                                |                                     | Some                       | One-way ANCOVA  |  |
|   | Multiple                       | Multiple                            | None                       | Factorial ANOVA   |  |
|   |                                |                                     | Some                       | Factorial ANCOVA  |  |
|   | Multiple                       | Multiple                            | One                        | One-way MANOVA or Hotelling's T square  |  |
|   |                                |                                     | Some                       | One-way MANCOVA   |  |
|   | Multiple                       | Multiple                            | None                       | Factorial MANOVA  |  |
|   |                                |                                     | Some                       | Factorial MANCOVA   |  |
|   | One                            | Multiple (one within S)             | None                       | Profile analysis of repeated measures   |  |
|   | Multiple (commensurate)        | One                                 | None                       | Profile analysis  |  |
|   | Multiple                       | Multiple (one within S)             | None                       | Doubly multivariate profile analysis  |  |
|   | Production of group membership | One (group differ on one attribute) | Multiple                   | None  |  |
| Some  |                                |                                     |                            | Hierarchical one-way discriminant function                                      |  |
| Multiple (groups differ on several attribute) |                                | Multiple                            | None                       | Factorial discriminant function   |  |
|   |                                |                                     | Some                       | Hierarchical factorial discriminant function                                    |  |
| Structure                                     | Multiple (observed)            | Multiple (latent)                   | None                       | Principal components (empirical)  | Create linear combinations of observed variables to represent latent variables |
|   |                                |                                     | Some                       | Factor analysis (theoretical)   |  |

**Table E Critical Values of Pearson r**

The values listed in the table are the critical values of r for the specified degrees of freedom (left column) and the alpha level (column heading). For two-tailed alpha levels,  $r_{crit}$  is both + and - To be significant,  $|r_{obs}| \geq |r_{crit}|$ .

| df - N - 2 | Level of Significance for One-Tailed Test |       |       |       |        |
|------------|---|-------|-------|-------|--------|
|            | .05                                       | .025  | .01   | .005  | .0005  |
|            | Level of Significance for Two-Tailed Test |       |       |       |        |
|            | .10                                       | .05   | .02   | .01   | .001   |
| 1          | .9877                                     | .9969 | .9995 | .9999 | 1.0000 |
| 2          | .9000                                     | .9500 | .9800 | .9900 | .9990  |
| 3          | .8054                                     | .8783 | .9343 | .9587 | .9912  |
| 4          | .7293                                     | .8114 | .8822 | .9172 | .9741  |
| 5          | .6694                                     | .7545 | .8329 | .8745 | .9507  |
| 6          | .6215                                     | .7067 | .7887 | .8343 | .9249  |
| 7          | .5822                                     | .6664 | .7498 | .7977 | .8982  |
| 8          | .5494                                     | .6319 | .7155 | .7646 | .8721  |
| 9          | .5214                                     | .6021 | .6851 | .7348 | .8471  |
| 10         | .4973                                     | .5760 | .6581 | .7079 | .8233  |
| 11         | .4762                                     | .5529 | .6339 | .6835 | .8010  |
| 12         | .4575                                     | .5324 | .6120 | .6611 | .7800  |
| 13         | .4409                                     | .5139 | .5923 | .6411 | .7603  |
| 14         | .4259                                     | .4973 | .5742 | .6226 | .7420  |
| 15         | .4124                                     | .4821 | .5577 | .6055 | .7246  |
| 16         | .4000                                     | .4683 | .5425 | .5897 | .7084  |
| 17         | .3887                                     | .4555 | .5285 | .5751 | .6932  |
| 18         | .3783                                     | .4438 | .5155 | .5614 | .6787  |
| 19         | .3687                                     | .4329 | .5034 | .5487 | .6652  |
| 20         | .3598                                     | .4227 | .4921 | .5368 | .6524  |
| 25         | .3233                                     | .3809 | .4451 | .4869 | .5974  |
| 30         | .2960                                     | .3494 | .4093 | .4487 | .5541  |
| 35         | .2746                                     | .3246 | .3810 | .4182 | .5189  |
| 40         | .2573                                     | .3044 | .3578 | .3932 | .4896  |
| 45         | .2428                                     | .2875 | .3384 | .3721 | .4648  |
| 50         | .2306                                     | .2732 | .3218 | .3541 | .4433  |
| 60         | .2108                                     | .2500 | .2948 | .3248 | .4078  |
| 70         | .1954                                     | .2319 | .2737 | .3017 | .3799  |
| 80         | .1829                                     | .2172 | .2565 | .2830 | .3568  |
| 90         | .1726                                     | .2050 | .2422 | .2673 | .3375  |
| 100        | .1638                                     | .1946 | .2301 | .2540 | .3211  |



**Table F (Continued)**

| Degrees of Freedom: Denominator | Degrees of Freedom: Numerator |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |  |  |
|---------------------------------|-------------------------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--|--|
|                                 | 1                             | 2            | 3            | 4            | 5            | 6            | 7            | 8            | 9            | 10           | 11           | 12           | 14           | 16           | 20           | 24           | 30           | 40           | 50           | 75           | 100          | 200          | 500          | ∞            |  |  |
| 20                              | 4.35<br>8.10                  | 3.49<br>5.85 | 3.10<br>4.94 | 2.87<br>4.43 | 2.71<br>4.10 | 2.60<br>3.87 | 2.52<br>3.71 | 2.45<br>3.56 | 2.40<br>3.45 | 2.35<br>3.37 | 2.31<br>3.30 | 2.28<br>3.23 | 2.23<br>3.13 | 2.18<br>3.05 | 2.12<br>2.94 | 2.08<br>2.84 | 2.04<br>2.77 | 1.99<br>2.69 | 1.96<br>2.63 | 1.92<br>2.56 | 1.90<br>2.53 | 1.87<br>2.47 | 1.85<br>2.44 | 1.84<br>2.42 |  |  |
| 21                              | 4.32<br>8.02                  | 3.47<br>5.78 | 3.07<br>4.87 | 2.84<br>4.37 | 2.68<br>4.04 | 2.57<br>3.81 | 2.49<br>3.65 | 2.42<br>3.51 | 2.37<br>3.40 | 2.32<br>3.31 | 2.28<br>3.24 | 2.25<br>3.17 | 2.20<br>3.07 | 2.15<br>2.99 | 2.09<br>2.88 | 2.05<br>2.80 | 2.00<br>2.72 | 1.96<br>2.63 | 1.93<br>2.58 | 1.89<br>2.51 | 1.87<br>2.47 | 1.84<br>2.42 | 1.82<br>2.38 | 1.81<br>2.36 |  |  |
| 22                              | 4.30<br>7.94                  | 3.44<br>5.72 | 3.05<br>4.82 | 2.82<br>4.31 | 2.66<br>3.99 | 2.55<br>3.78 | 2.47<br>3.59 | 2.40<br>3.45 | 2.35<br>3.35 | 2.30<br>3.26 | 2.26<br>3.18 | 2.23<br>3.12 | 2.18<br>3.02 | 2.13<br>2.94 | 2.07<br>2.83 | 2.03<br>2.75 | 2.00<br>2.67 | 1.98<br>2.58 | 1.93<br>2.53 | 1.91<br>2.46 | 1.87<br>2.42 | 1.84<br>2.37 | 1.81<br>2.32 | 1.80<br>2.31 |  |  |
| 23                              | 4.28<br>7.88                  | 3.42<br>5.68 | 3.03<br>4.76 | 2.80<br>4.26 | 2.64<br>3.94 | 2.53<br>3.71 | 2.45<br>3.54 | 2.38<br>3.41 | 2.32<br>3.30 | 2.28<br>3.21 | 2.24<br>3.14 | 2.20<br>3.07 | 2.14<br>2.97 | 2.10<br>2.89 | 2.04<br>2.78 | 2.00<br>2.70 | 1.96<br>2.62 | 1.91<br>2.53 | 1.88<br>2.48 | 1.84<br>2.41 | 1.82<br>2.37 | 1.79<br>2.32 | 1.77<br>2.28 | 1.76<br>2.26 |  |  |
| 24                              | 4.26<br>7.82                  | 3.40<br>5.61 | 3.01<br>4.72 | 2.78<br>4.22 | 2.62<br>3.90 | 2.51<br>3.67 | 2.43<br>3.50 | 2.36<br>3.36 | 2.30<br>3.25 | 2.26<br>3.17 | 2.22<br>3.09 | 2.18<br>3.03 | 2.13<br>2.93 | 2.09<br>2.85 | 2.02<br>2.74 | 1.98<br>2.66 | 1.94<br>2.58 | 1.89<br>2.48 | 1.86<br>2.44 | 1.82<br>2.38 | 1.80<br>2.33 | 1.76<br>2.27 | 1.74<br>2.23 | 1.73<br>2.21 |  |  |
| 25                              | 4.24<br>7.77                  | 3.38<br>5.57 | 2.99<br>4.66 | 2.76<br>4.18 | 2.60<br>3.86 | 2.49<br>3.63 | 2.41<br>3.46 | 2.34<br>3.32 | 2.28<br>3.21 | 2.24<br>3.13 | 2.20<br>3.05 | 2.16<br>2.98 | 2.11<br>2.89 | 2.06<br>2.81 | 2.00<br>2.70 | 1.96<br>2.62 | 1.92<br>2.54 | 1.87<br>2.45 | 1.84<br>2.40 | 1.80<br>2.32 | 1.77<br>2.29 | 1.74<br>2.23 | 1.72<br>2.19 | 1.71<br>2.17 |  |  |
| 26                              | 4.22<br>7.72                  | 3.37<br>5.53 | 2.98<br>4.64 | 2.74<br>4.14 | 2.59<br>3.82 | 2.47<br>3.59 | 2.39<br>3.42 | 2.32<br>3.29 | 2.27<br>3.17 | 2.22<br>3.09 | 2.18<br>3.02 | 2.15<br>2.96 | 2.10<br>2.86 | 2.05<br>2.77 | 1.99<br>2.66 | 1.95<br>2.58 | 1.90<br>2.50 | 1.85<br>2.41 | 1.82<br>2.36 | 1.78<br>2.28 | 1.76<br>2.25 | 1.72<br>2.19 | 1.70<br>2.15 | 1.69<br>2.13 |  |  |
| 27                              | 4.21<br>7.68                  | 3.35<br>5.49 | 2.96<br>4.60 | 2.73<br>4.11 | 2.57<br>3.79 | 2.46<br>3.56 | 2.37<br>3.39 | 2.30<br>3.26 | 2.25<br>3.14 | 2.20<br>3.06 | 2.16<br>2.98 | 2.13<br>2.93 | 2.08<br>2.83 | 2.03<br>2.74 | 1.97<br>2.63 | 1.93<br>2.55 | 1.88<br>2.47 | 1.84<br>2.38 | 1.80<br>2.32 | 1.76<br>2.25 | 1.74<br>2.21 | 1.71<br>2.16 | 1.68<br>2.12 | 1.67<br>2.10 |  |  |
| 28                              | 4.20<br>7.64                  | 3.34<br>5.45 | 2.95<br>4.57 | 2.71<br>4.07 | 2.56<br>3.76 | 2.44<br>3.53 | 2.36<br>3.36 | 2.29<br>3.23 | 2.24<br>3.11 | 2.19<br>3.03 | 2.15<br>2.95 | 2.12<br>2.89 | 2.06<br>2.80 | 2.02<br>2.71 | 1.96<br>2.60 | 1.91<br>2.52 | 1.87<br>2.44 | 1.81<br>2.35 | 1.78<br>2.30 | 1.75<br>2.22 | 1.72<br>2.18 | 1.69<br>2.13 | 1.67<br>2.09 | 1.65<br>2.06 |  |  |
| 29                              | 4.18<br>7.60                  | 3.33<br>5.42 | 2.93<br>4.54 | 2.70<br>4.04 | 2.54<br>3.73 | 2.43<br>3.50 | 2.35<br>3.33 | 2.28<br>3.20 | 2.22<br>3.08 | 2.18<br>3.00 | 2.14<br>2.92 | 2.10<br>2.87 | 2.05<br>2.77 | 2.00<br>2.68 | 1.94<br>2.57 | 1.90<br>2.49 | 1.85<br>2.41 | 1.80<br>2.32 | 1.77<br>2.23 | 1.73<br>2.19 | 1.71<br>2.15 | 1.68<br>2.10 | 1.64<br>2.06 | 1.64<br>2.03 |  |  |
| 30                              | 4.17<br>7.58                  | 3.32<br>5.39 | 2.92<br>4.51 | 2.69<br>4.02 | 2.53<br>3.70 | 2.42<br>3.47 | 2.34<br>3.30 | 2.27<br>3.17 | 2.21<br>3.06 | 2.16<br>2.98 | 2.12<br>2.90 | 2.09<br>2.84 | 2.04<br>2.74 | 1.99<br>2.66 | 1.93<br>2.55 | 1.89<br>2.47 | 1.84<br>2.38 | 1.79<br>2.28 | 1.76<br>2.24 | 1.72<br>2.18 | 1.69<br>2.13 | 1.66<br>2.07 | 1.64<br>2.03 | 1.62<br>2.01 |  |  |
| 32                              | 4.15<br>7.56                  | 3.29<br>5.34 | 2.90<br>4.46 | 2.67<br>3.97 | 2.51<br>3.66 | 2.40<br>3.42 | 2.32<br>3.25 | 2.25<br>3.12 | 2.19<br>3.01 | 2.14<br>2.94 | 2.10<br>2.86 | 2.07<br>2.80 | 2.02<br>2.70 | 1.97<br>2.62 | 1.91<br>2.51 | 1.86<br>2.42 | 1.82<br>2.34 | 1.76<br>2.25 | 1.74<br>2.20 | 1.69<br>2.12 | 1.67<br>2.08 | 1.64<br>2.02 | 1.61<br>1.98 | 1.59<br>1.96 |  |  |
| 34                              | 4.13<br>7.44                  | 3.28<br>5.29 | 2.88<br>4.42 | 2.65<br>3.93 | 2.49<br>3.61 | 2.38<br>3.38 | 2.30<br>3.21 | 2.23<br>3.08 | 2.17<br>2.97 | 2.12<br>2.89 | 2.08<br>2.82 | 2.05<br>2.75 | 2.00<br>2.66 | 1.95<br>2.58 | 1.89<br>2.47 | 1.84<br>2.38 | 1.80<br>2.30 | 1.74<br>2.21 | 1.71<br>2.15 | 1.67<br>2.08 | 1.64<br>2.04 | 1.61<br>1.98 | 1.59<br>1.94 | 1.57<br>1.91 |  |  |
| 36                              | 4.11<br>7.38                  | 3.26<br>5.25 | 2.86<br>4.38 | 2.63<br>3.89 | 2.48<br>3.58 | 2.36<br>3.35 | 2.28<br>3.18 | 2.21<br>3.04 | 2.15<br>2.94 | 2.10<br>2.86 | 2.06<br>2.78 | 2.03<br>2.72 | 1.98<br>2.62 | 1.93<br>2.54 | 1.87<br>2.43 | 1.82<br>2.35 | 1.78<br>2.26 | 1.72<br>2.17 | 1.69<br>2.12 | 1.65<br>2.04 | 1.62<br>2.00 | 1.59<br>1.94 | 1.56<br>1.90 | 1.55<br>1.87 |  |  |
| 38                              | 4.10<br>7.35                  | 3.25<br>5.21 | 2.85<br>4.34 | 2.62<br>3.88 | 2.46<br>3.54 | 2.35<br>3.32 | 2.26<br>3.15 | 2.19<br>3.02 | 2.14<br>2.91 | 2.09<br>2.82 | 2.05<br>2.75 | 2.02<br>2.69 | 1.96<br>2.58 | 1.92<br>2.51 | 1.85<br>2.40 | 1.80<br>2.32 | 1.76<br>2.22 | 1.71<br>2.14 | 1.67<br>2.08 | 1.63<br>2.00 | 1.60<br>1.97 | 1.57<br>1.90 | 1.54<br>1.86 | 1.53<br>1.84 |  |  |
| 40                              | 4.08<br>7.31                  | 3.23<br>5.18 | 2.84<br>4.31 | 2.61<br>3.83 | 2.45<br>3.51 | 2.34<br>3.29 | 2.25<br>3.12 | 2.18<br>2.99 | 2.12<br>2.88 | 2.07<br>2.80 | 2.04<br>2.73 | 2.00<br>2.66 | 1.95<br>2.56 | 1.90<br>2.48 | 1.84<br>2.37 | 1.79<br>2.29 | 1.74<br>2.20 | 1.69<br>2.11 | 1.66<br>2.05 | 1.61<br>1.97 | 1.58<br>1.94 | 1.55<br>1.88 | 1.53<br>1.84 | 1.51<br>1.81 |  |  |
| 42                              | 4.07<br>7.27                  | 3.22<br>5.15 | 2.83<br>4.29 | 2.59<br>3.80 | 2.44<br>3.49 | 2.32<br>3.26 | 2.24<br>3.10 | 2.17<br>2.96 | 2.11<br>2.86 | 2.06<br>2.77 | 2.02<br>2.70 | 1.99<br>2.64 | 1.94<br>2.54 | 1.89<br>2.46 | 1.82<br>2.35 | 1.78<br>2.26 | 1.73<br>2.17 | 1.68<br>2.08 | 1.64<br>2.02 | 1.60<br>1.94 | 1.57<br>1.91 | 1.54<br>1.85 | 1.51<br>1.80 | 1.49<br>1.78 |  |  |
| 44                              | 4.06<br>7.24                  | 3.21<br>5.12 | 2.82<br>4.28 | 2.58<br>3.78 | 2.43<br>3.46 | 2.31<br>3.24 | 2.23<br>3.07 | 2.16<br>2.94 | 2.10<br>2.84 | 2.05<br>2.75 | 2.01<br>2.68 | 1.98<br>2.62 | 1.92<br>2.52 | 1.88<br>2.44 | 1.81<br>2.32 | 1.76<br>2.24 | 1.72<br>2.15 | 1.66<br>2.06 | 1.63<br>2.00 | 1.58<br>1.92 | 1.56<br>1.88 | 1.52<br>1.82 | 1.50<br>1.80 | 1.48<br>1.78 |  |  |
| 46                              | 4.05<br>7.21                  | 3.20<br>5.10 | 2.81<br>4.24 | 2.57<br>3.76 | 2.42<br>3.44 | 2.30<br>3.22 | 2.23<br>3.05 | 2.14<br>2.92 | 2.09<br>2.82 | 2.04<br>2.73 | 2.00<br>2.66 | 1.97<br>2.60 | 1.91<br>2.50 | 1.87<br>2.42 | 1.80<br>2.30 | 1.75<br>2.22 | 1.71<br>2.13 | 1.65<br>2.04 | 1.62<br>1.98 | 1.57<br>1.90 | 1.54<br>1.86 | 1.51<br>1.80 | 1.48<br>1.76 | 1.46<br>1.72 |  |  |
| 48                              | 4.04<br>7.19                  | 3.19<br>5.08 | 2.80<br>4.22 | 2.56<br>3.74 | 2.41<br>3.42 | 2.30<br>3.28 | 2.21<br>3.04 | 2.14<br>2.90 | 2.08<br>2.80 | 2.03<br>2.71 | 1.99<br>2.64 | 1.96<br>2.58 | 1.90<br>2.48 | 1.86<br>2.40 | 1.79<br>2.28 | 1.74<br>2.20 | 1.70<br>2.11 | 1.64<br>2.02 | 1.61<br>1.96 | 1.56<br>1.88 | 1.53<br>1.84 | 1.50<br>1.78 | 1.47<br>1.73 | 1.45<br>1.70 |  |  |
| 50                              | 4.03<br>7.17                  | 3.18<br>5.06 | 2.79<br>4.20 | 2.56<br>3.72 | 2.40<br>3.41 | 2.29<br>3.18 | 2.20<br>3.02 | 2.13<br>2.88 | 2.07<br>2.78 | 2.02<br>2.70 | 1.98<br>2.62 | 1.95<br>2.56 | 1.90<br>2.46 | 1.85<br>2.39 | 1.78<br>2.28 | 1.74<br>2.18 | 1.69<br>2.10 | 1.63<br>2.00 | 1.60<br>1.94 | 1.55<br>1.86 | 1.52<br>1.82 | 1.48<br>1.76 | 1.46<br>1.71 | 1.44<br>1.68 |  |  |
| 55                              | 4.02<br>7.12                  | 3.17<br>5.01 | 2.78<br>4.18 | 2.54<br>3.68 | 2.38<br>3.37 | 2.27<br>3.15 | 2.18<br>2.98 | 2.11<br>2.85 | 2.05<br>2.75 | 2.00<br>2.66 | 1.97<br>2.59 | 1.93<br>2.53 | 1.88<br>2.43 | 1.83<br>2.35 | 1.76<br>2.23 | 1.72<br>2.15 | 1.67<br>2.06 | 1.61<br>1.96 | 1.58<br>1.90 | 1.52<br>1.82 | 1.50<br>1.78 | 1.46<br>1.71 | 1.43<br>1.66 | 1.41<br>1.64 |  |  |
| 60                              | 4.00<br>7.08                  | 3.15<br>4.98 | 2.76<br>4.13 | 2.52<br>3.65 | 2.37<br>3.34 | 2.25<br>3.12 | 2.17<br>2.95 | 2.10<br>2.82 | 2.04<br>2.72 | 1.99<br>2.63 | 1.95<br>2.56 | 1.92<br>2.50 | 1.86<br>2.40 | 1.81<br>2.32 | 1.75<br>2.20 | 1.70<br>2.12 | 1.65<br>2.03 | 1.59<br>1.93 | 1.56<br>1.87 | 1.50<br>1.79 | 1.48<br>1.74 | 1.44<br>1.68 | 1.41<br>1.63 | 1.39<br>1.60 |  |  |
| 65                              | 3.99<br>7.04                  | 3.14<br>4.95 | 2.75<br>4.10 | 2.51<br>3.62 | 2.36<br>3.31 | 2.24<br>3.09 | 2.15<br>2.93 | 2.08<br>2.79 | 2.02<br>2.70 | 1.98<br>2.61 | 1.94<br>2.54 | 1.90<br>2.47 | 1.85<br>2.37 | 1.80<br>2.30 | 1.73<br>2.18 | 1.68<br>2.09 | 1.63<br>2.00 | 1.57<br>1.90 | 1.54<br>1.84 | 1.49<br>1.76 | 1.46<br>1.71 | 1.42<br>1.64 | 1.39<br>1.60 | 1.37<br>1.56 |  |  |
| 70                              | 3.98<br>7.01                  | 3.13<br>4.92 | 2.74<br>4.08 | 2.50<br>3.60 | 2.35<br>3.29 | 2.23<br>3.07 | 2.14<br>2.91 | 2.07<br>2.77 | 2.01<br>2.67 | 1.97<br>2.60 | 1.93<br>2.51 | 1.89<br>2.45 | 1.84<br>2.36 | 1.79<br>2.28 | 1.72<br>2.15 | 1.67<br>2.07 | 1.62<br>1.98 | 1.56<br>1.88 | 1.53<br>1.82 | 1.47<br>1.74 | 1.45<br>1.69 | 1.40<br>1.62 | 1.37<br>1.53 | 1.35<br>1.53 |  |  |
| 80                              | 3.96<br>6.96                  | 3.11<br>4.88 | 2.72<br>4.04 | 2.48<br>3.56 | 2.33<br>3.25 | 2.21<br>3.04 | 2.12<br>2.87 | 2.05<br>2.74 | 1.99<br>2.64 | 1.95<br>2.55 | 1.91<br>2.48 | 1.88<br>2.41 | 1.82<br>2.32 | 1.77<br>2.24 | 1.70<br>2.11 | 1.65<br>2.03 | 1.60<br>1.94 | 1.54<br>1.84 | 1.51<br>1.78 | 1.45<br>1.70 | 1.42<br>1.65 | 1.38<br>1.57 | 1.35<br>1.52 | 1.32<br>1.49 |  |  |

**Table F (Continued)**

| Degrees of Freedom: Denominator | Degrees of Freedom: Numerator |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |                     |
|---------------------------------|-------------------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
|                                 | 1                             | 2                   | 3                   | 4                   | 5                   | 6                   | 7                   | 8                   | 9                   | 10                  | 11                  | 12                  | 14                  | 16                  | 20                  | 24                  | 30                  | 40                  | 50                  | 75                  | 100                 | 200                 | 500                 | $\infty$            |
| 100                             | 3.94<br><b>6.90</b>           | 3.09<br><b>4.82</b> | 2.70<br><b>3.98</b> | 2.46<br><b>3.51</b> | 2.30<br><b>3.20</b> | 2.19<br><b>2.99</b> | 2.10<br><b>2.82</b> | 2.03<br><b>2.69</b> | 1.97<br><b>2.59</b> | 1.92<br><b>2.51</b> | 1.88<br><b>2.43</b> | 1.85<br><b>2.36</b> | 1.79<br><b>2.28</b> | 1.75<br><b>2.19</b> | 1.68<br><b>2.06</b> | 1.63<br><b>1.98</b> | 1.57<br><b>1.89</b> | 1.51<br><b>1.79</b> | 1.48<br><b>1.73</b> | 1.42<br><b>1.64</b> | 1.39<br><b>1.59</b> | 1.34<br><b>1.51</b> | 1.30<br><b>1.46</b> | 1.28<br><b>1.43</b> |
| 125                             | 3.92<br><b>6.84</b>           | 3.07<br><b>4.78</b> | 2.68<br><b>3.84</b> | 2.44<br><b>3.47</b> | 2.29<br><b>3.17</b> | 2.17<br><b>2.85</b> | 2.08<br><b>2.78</b> | 2.01<br><b>2.65</b> | 1.95<br><b>2.56</b> | 1.90<br><b>2.47</b> | 1.86<br><b>2.40</b> | 1.83<br><b>2.33</b> | 1.77<br><b>2.23</b> | 1.72<br><b>2.15</b> | 1.65<br><b>2.03</b> | 1.60<br><b>1.94</b> | 1.55<br><b>1.85</b> | 1.49<br><b>1.75</b> | 1.45<br><b>1.68</b> | 1.39<br><b>1.59</b> | 1.36<br><b>1.54</b> | 1.31<br><b>1.46</b> | 1.27<br><b>1.40</b> | 1.25<br><b>1.37</b> |
| 150                             | 3.91<br><b>6.81</b>           | 3.06<br><b>4.75</b> | 2.67<br><b>3.81</b> | 2.43<br><b>3.44</b> | 2.27<br><b>3.14</b> | 2.16<br><b>2.82</b> | 2.07<br><b>2.76</b> | 2.00<br><b>2.62</b> | 1.94<br><b>2.53</b> | 1.89<br><b>2.44</b> | 1.85<br><b>2.37</b> | 1.82<br><b>2.30</b> | 1.76<br><b>2.20</b> | 1.71<br><b>2.12</b> | 1.64<br><b>2.00</b> | 1.59<br><b>1.91</b> | 1.54<br><b>1.83</b> | 1.47<br><b>1.72</b> | 1.44<br><b>1.66</b> | 1.37<br><b>1.56</b> | 1.34<br><b>1.51</b> | 1.29<br><b>1.43</b> | 1.25<br><b>1.37</b> | 1.22<br><b>1.33</b> |
| 200                             | 3.89<br><b>6.76</b>           | 3.04<br><b>4.71</b> | 2.65<br><b>3.88</b> | 2.41<br><b>3.41</b> | 2.26<br><b>3.11</b> | 2.14<br><b>2.99</b> | 2.05<br><b>2.73</b> | 1.98<br><b>2.60</b> | 1.92<br><b>2.56</b> | 1.87<br><b>2.41</b> | 1.83<br><b>2.34</b> | 1.80<br><b>2.28</b> | 1.74<br><b>2.17</b> | 1.69<br><b>2.09</b> | 1.62<br><b>1.97</b> | 1.57<br><b>1.88</b> | 1.52<br><b>1.79</b> | 1.45<br><b>1.69</b> | 1.42<br><b>1.60</b> | 1.35<br><b>1.53</b> | 1.32<br><b>1.48</b> | 1.26<br><b>1.39</b> | 1.22<br><b>1.33</b> | 1.19<br><b>1.28</b> |
| 400                             | 3.86<br><b>6.70</b>           | 3.02<br><b>4.66</b> | 2.62<br><b>3.83</b> | 2.39<br><b>3.36</b> | 2.23<br><b>3.06</b> | 2.12<br><b>2.85</b> | 2.03<br><b>2.69</b> | 1.96<br><b>2.55</b> | 1.90<br><b>2.46</b> | 1.85<br><b>2.37</b> | 1.81<br><b>2.29</b> | 1.78<br><b>2.23</b> | 1.72<br><b>2.12</b> | 1.67<br><b>2.04</b> | 1.60<br><b>1.92</b> | 1.54<br><b>1.84</b> | 1.49<br><b>1.74</b> | 1.42<br><b>1.64</b> | 1.38<br><b>1.57</b> | 1.32<br><b>1.47</b> | 1.28<br><b>1.42</b> | 1.22<br><b>1.32</b> | 1.16<br><b>1.24</b> | 1.13<br><b>1.19</b> |
| 1000                            | 3.85<br><b>6.66</b>           | 3.00<br><b>4.62</b> | 2.61<br><b>3.80</b> | 2.38<br><b>3.34</b> | 2.22<br><b>3.04</b> | 2.10<br><b>2.82</b> | 2.02<br><b>2.66</b> | 1.95<br><b>2.53</b> | 1.89<br><b>2.43</b> | 1.84<br><b>2.34</b> | 1.80<br><b>2.26</b> | 1.76<br><b>2.20</b> | 1.70<br><b>2.09</b> | 1.65<br><b>2.01</b> | 1.58<br><b>1.89</b> | 1.53<br><b>1.81</b> | 1.47<br><b>1.71</b> | 1.41<br><b>1.61</b> | 1.36<br><b>1.54</b> | 1.30<br><b>1.44</b> | 1.26<br><b>1.38</b> | 1.19<br><b>1.28</b> | 1.13<br><b>1.19</b> | 1.08<br><b>1.11</b> |
| $\infty$                        | 3.84<br><b>6.64</b>           | 2.99<br><b>4.60</b> | 2.60<br><b>3.78</b> | 2.37<br><b>3.32</b> | 2.21<br><b>3.02</b> | 2.09<br><b>2.80</b> | 2.01<br><b>2.64</b> | 1.94<br><b>2.51</b> | 1.88<br><b>2.41</b> | 1.83<br><b>2.32</b> | 1.79<br><b>2.24</b> | 1.75<br><b>2.18</b> | 1.69<br><b>2.07</b> | 1.64<br><b>1.99</b> | 1.57<br><b>1.87</b> | 1.52<br><b>1.79</b> | 1.46<br><b>1.69</b> | 1.40<br><b>1.59</b> | 1.35<br><b>1.52</b> | 1.28<br><b>1.41</b> | 1.24<br><b>1.36</b> | 1.17<br><b>1.25</b> | 1.11<br><b>1.15</b> | 1.00<br><b>1.00</b> |

**Table Q Random Numbers**

|    | 1                  | 2            | 3            | 4            | 5            | 6            | 7            | 8            | 9            |
|----|--------------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| 1  | 32942              | <b>95416</b> | 42339        | 59045        | 26693        | 49057        | <b>87496</b> | <b>20624</b> | <b>14819</b> |
| 2  | <b>07410/99859</b> |              | 83828        | <b>21409</b> | <b>29094</b> | <b>65114</b> | <b>36701</b> | <b>25762</b> | <b>12827</b> |
| 3  | <b>59981</b>       | <b>68155</b> | <b>45673</b> | <b>76210</b> | <b>58219</b> | <b>45738</b> | <b>29550</b> | <b>24736</b> | <b>09574</b> |
| 4  | 46251              | 25437        | 69654        | 99716        | <b>11563</b> | 08803        | 86027        | <b>51867</b> | <b>12116</b> |
| 5  | 65558              | 51904        | 93123        | 27887        | <b>53138</b> | <b>21488</b> | 09095        | 787-i        | <b>71240</b> |
| 6  | 99187              | 19258        | <b>86421</b> | <b>16401</b> | 19397        | 83297        | <b>40111</b> | 49326        | 81686        |
| 7  | <b>35641</b>       | 00301        | 16096        | 34775        | 21562        | 97983        | 45040        | <b>19200</b> | 16383        |
| 8  | 14031              | 00936        | 81518        | 48440        | <b>02218</b> | 04756        | 19506        | 60695        | 88494        |
| 9  | 60677              | 15076        | 92554        | 26042        | 23472        | 69869        | 62877        | 19584        | 39576        |
| 10 | 66314              | <b>05212</b> | <b>67859</b> | <b>89356</b> | <b>20056</b> | 30648        | 87349        | 10389        | 53805        |
| 11 | 20416              | <b>87410</b> | 75646        | <b>64176</b> | <b>82752</b> | 63606        | 37011        | 37346        | 69512        |
| 12 | 28701              | 56992        | 70423        | 62415        | 10807        | 98086        | <b>58850</b> | <b>28968</b> | 45297        |
| 13 | 74579              | 33844        | 33426        | 07570        | <b>00728</b> | 07079        | 19322        | 56325        | 84819        |
| 14 | <b>62615</b>       | 52342        | 82968        | 75540        | <b>80045</b> | 53069        | 20665        | <b>21282</b> | 07768        |
| 15 | 93945              | 06293        | <b>22879</b> | 08161        | 01442        | 75071        | <b>21427</b> | <b>94842</b> | 26210        |
| 16 | 75689              | <b>76131</b> | 96837        | 67450        | <b>44511</b> | 50424        | 82848        | 41975        | 71663        |
| 17 | 02921              | 16919        | 35424        | <b>93209</b> | <b>52133</b> | <b>87327</b> | 95897        | <b>65171</b> | 10376        |
| 18 | 14295              | 34969        | 14216        | 03191        | 61647        | 30296        | 66667        | <b>10101</b> | 63203        |
| 19 | 05303              | 91109        | 82403        | <b>40312</b> | 62191        | 67023        | 90073        | 33205        | 71344        |
| 20 | 57071              | 90357        | <b>12901</b> | 08899        | <b>91039</b> | <b>67251</b> | <b>28701</b> | <b>03846</b> | 94589        |
| 21 | 78471              | 57741        | 13599        | 84390        | 32146        | 00871        | <b>09354</b> | 22745        | 65806        |
| 22 | 89242              | 79337        | 59293        | 47481        | 07740        | 43345        | <b>25716</b> | 70020        | <b>54005</b> |
| 23 | <b>14955</b>       | 59592        | 97035        | 90430        | 87220        | 06392        | <b>79028</b> | <b>57123</b> | <b>52872</b> |
| 24 | 42446              | <b>41880</b> | <b>37415</b> | 47472        | 04513        | 49494        | 08860        | 08038        | 43624        |
| 25 | 18534              | 22346        | 54556        | <b>17558</b> | 73689        | <b>14894</b> | 05030        | 19561        | 56517        |
| 26 | 39284              | 33737        | <b>42512</b> | <b>86411</b> | 23753        | <b>29690</b> | <b>26096</b> | <b>81361</b> | 93099        |
| 27 | 33922              | 37329        | 89911        | <b>55876</b> | <b>28379</b> | <b>81031</b> | <b>22058</b> | <b>21487</b> | <b>54613</b> |
| 28 | <b>78355</b>       | <b>54013</b> | 50774        | 30666        | 61205        | <b>42574</b> | <b>47773</b> | 36027        | 27174        |
| 29 | 08845              | 99145        | 94316        | 88974        | <b>29828</b> | <b>97069</b> | 90327        | 61842        | 29604        |
| 30 | 01769              | <b>71825</b> | 55957        | 98271        | 02784        | 66731        | <b>40311</b> | <b>88495</b> | <b>18821</b> |
| 31 | 17639              | 38284        | 59478        | 90409        | <b>21997</b> | 56199        | <b>30068</b> | <b>82800</b> | 69692        |
| 32 | <b>05851</b>       | 58653        | 99949        | 63505        | 40409        | <b>85551</b> | 90729        | 64938        | 52403        |
| 33 | 42396              | <b>40112</b> | <b>11469</b> | 03476        | 03328        | 84238        | 26570        | 51790        | <b>42122</b> |
| 34 | <b>13318</b>       | 14192        | 98167        | <b>75631</b> | <b>74141</b> | 22369        | 36757        | <b>89117</b> | 54998        |
| 35 | 60571              | 54786        | 26281        | <b>01855</b> | 30706        | <b>66578</b> | 32019        | <b>65884</b> | <b>58485</b> |
| 36 | 09531              | 81853        | 59334        | 70929        | 03544        | <b>18510</b> | <b>89541</b> | <b>13555</b> | 21168        |
| 37 | <b>72865</b>       | 16829        | 86542        | <b>00396</b> | 20363        | 13010        | 69645        | 49608        | 54738        |
| 38 | 56324              | 31093        | 77924        | 28622        | 83543        | 28912        | 15059        | <b>80192</b> | a3964        |
| 39 | 78192              | <b>21626</b> | 91399        | 07235        | 07104        | 73652        | 64425        | <b>85149</b> | 75409        |
| 40 | 84666              | 34767        | 97298        | 92708        | 01994        | 53188        | 78476        | 07804        | 62404        |
| 41 | <b>82201</b>       | 75694        | 02808        | 65983        | <b>74373</b> | 66693        | 13094        | <b>74183</b> | 73020        |
| 42 | 15360              | 73776        | 40914        | 85190        | <b>54278</b> | 99054        | 62944        | 47351        | 89098        |
| 43 | 68142              | 67957        | 70896        | 37983        | 20487        | 95350        | <b>16371</b> | <b>03426</b> | 13895        |
| 44 | 19138              | 31200        | 30616        | 14639        | 44406        | 44236        | 57360        | <b>81644</b> | 94761        |
| 45 | <b>28155</b>       | 03521        | <b>36415</b> | 78452        | 92359        | 81091        | 56513        | 88321        | 97910        |
| 46 | <b>87971</b>       | 29031        | 51780        | 27376        | 81056        | <b>86155</b> | 55488        | 50590        | 74514        |
| 47 | 58147              | <b>68841</b> | <b>53625</b> | 02059        | 75223        | 16783        | <b>19272</b> | 61994        | 71090        |
| 48 | 18875              | 52809        | 70594        | 41649        | 32935        | 26430        | 82096        | 01605        | 65846        |
| 49 | 75109              | 56474        | <b>74111</b> | 31966        | 29969        | <b>70093</b> | 98901        | 84550        | 25769        |
| 50 | 35983              | 03742        | 76822        | 12073        | 59463        | X4420        | 15868        | 99505        | 11426        |

|    |       |       |       |        |       |       |        |
|----|-------|-------|-------|--------|-------|-------|--------|
|    |       |       |       |        | 07469 | 42341 | 98173  |
|    |       |       |       |        | 09343 | 70278 | 67331  |
|    |       |       |       |        | 05610 | 53750 | 95938  |
|    |       | 24127 |       |        | 73977 | 95218 | 96074  |
|    |       |       | 23045 |        | 1597  | 60012 | 98866  |
|    |       |       |       |        | 51378 | 08360 | 95946  |
|    |       | 02238 |       | 21219  | 87817 | 41705 | 95785  |
|    |       |       |       | 83612  | 4     | 1540  | 86492  |
|    |       |       |       | 78185  | 62154 | 77930 | 67663  |
|    |       |       |       |        |       |       | 29529  |
|    |       | 07779 | 04157 | 41172  | 36473 | 42123 | 43929  |
|    |       | 06596 | 48416 | 69770  | 68797 | 56080 | 14223  |
|    |       | 62742 | 14891 | 39247  | 51242 | 98832 | 69533  |
|    |       | 54976 | 48957 | 74599  | 08751 | 78494 | 52785  |
|    |       | 78033 | 66885 | 13936  | 42117 | 71831 | 22961  |
|    |       | 53850 | 32827 | 81647  | 80820 | 00420 | 63555  |
|    |       | 88562 | 70745 | 23701  | 45630 | 65891 | 5820   |
|    |       | 7384  | 90199 | 79210  | 76965 | 99546 | 30323  |
|    |       | 48951 | 53674 | 17880  | 45260 | 08575 | 49321  |
|    |       | 84221 | 78902 | 82010  | 30847 | 62329 | 63898  |
|    |       | 69704 | 82267 | 14751  | 13151 | 931   | 15     |
|    |       | 4846  | 59278 | 4418.1 | 29616 | 76531 | 19589  |
|    |       | 14073 | 07026 | 25264  | 08388 | 27182 | 22557  |
|    |       | 57181 | 10238 | 3hR7.1 | 28546 | 37444 | 80824  |
|    |       | 86245 | 32623 | 78858  | 08143 | 60377 | 42925  |
|    |       | 13592 | 60642 | 17904  | 99718 | 63432 | 88642  |
|    |       | 23900 | 48761 | 44860  | 92467 | 31742 | 87142  |
|    |       | 07489 | 85986 | 74420  | 2,744 | 977   | 11     |
|    |       | 03711 | 63824 | 07953  | 85965 | 87089 | 11687  |
|    |       | 91946 | 78437 | 34365  | 87469 | 12430 | 84754  |
|    |       | 27534 | 88913 | 49055  | 19218 | 47712 | 67677  |
|    | 08833 | 42549 | 93981 | 4X382  | 83725 | 72643 | 64233  |
|    |       | 11139 | 47479 | 9      | 1560  | 95372 | 97642  |
|    | 62032 |       | 75478 | 52726  | 30289 | 42411 | 91886  |
| 35 |       |       | 53116 | 58301  | 24375 | 65609 | 85810  |
|    | 91611 |       | 60128 | 63698  | 78356 | 50662 | 22505  |
|    |       |       | 86314 | 93582  | 73604 | 78614 | 78849  |
| 38 |       |       | 74091 | 10970  | 8657  | 65661 | 41854  |
| 39 | 02955 |       | 90288 | 83646  | 94435 | 06560 | 78029  |
| 40 | 55608 |       | 82767 | 74646  | 79485 | 13619 | 98866  |
| 41 | 17831 |       | 79473 | 28394  | 79334 | 70577 | 38048  |
| 42 |       |       | 07585 | 1117X  | 32601 | 27994 | 05641  |
| 43 | 31343 |       | 14576 | 16039  | 47517 | 43300 | 59080  |
| 44 |       |       | 40103 | 05635  | 81673 | 68657 | 09559  |
| 45 | 52934 |       | 26499 | 67331  | 80993 | 61299 | 36979  |
| 46 | 58552 |       | 07678 | 6537   | 30705 | 99582 | 53390. |
| 47 |       |       | 87131 | 47946  | 09854 | 18080 | 02321  |
| 48 |       |       | 44916 | 89717  | 88189 | 30143 | 52687  |
| 49 | 98642 | 89822 | 71691 | 83666  | 61642 | 46683 | 3376   |
| 30 | 60139 | 25601 | 93663 | 02654  | 94824 | 48672 | 28736  |

