

ภาคผนวก 2

สูตรพื้นฐาน

I

$$\sin^2\theta + \cos^2\theta = 1$$

$$\tan^2\theta + 1 = \sec^2\theta$$

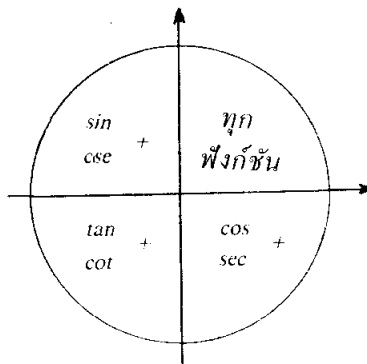
$$\cot^2\theta + 1 = \csc^2\theta$$

II

| ฟังก์ชัน \ มุม | 0° | 30° | 45° | 60° | 90° | 180° | 270° |
|----------------|----|----------------------|----------------------|----------------------|-------------|------|-------------|
| sine | 0 | $\frac{1}{2}$ | $\frac{1}{\sqrt{2}}$ | $\frac{\sqrt{3}}{2}$ | 1 | 0 | -1 |
| cosine | 1 | $\frac{\sqrt{3}}{2}$ | $\frac{1}{\sqrt{2}}$ | $\frac{1}{2}$ | 0 | -1 | 0 |
| tangent | 0 | $\frac{1}{\sqrt{3}}$ | 1 | $\sqrt{3}$ | หาค่าไม่ได้ | 0 | หาค่าไม่ได้ |

หมายเหตุ $30^\circ = \frac{\pi}{6}$, $45^\circ = \frac{\pi}{4}$, $60^\circ = \frac{\pi}{3}$, $90^\circ = \frac{\pi}{2}$, $180^\circ = \pi$, $270^\circ = \frac{3\pi}{2}$, $360^\circ = 2\pi$

III



IV

| | |
|-------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| จตุภาคที่ 2 | $\sin(180^\circ - \theta) = +\sin \theta$ $\cos(180^\circ - \theta) = -\cos \theta$ $\tan(180^\circ - \theta) = -\tan \theta$ |
| จตุภาคที่ 3 | $\sin(180^\circ + \theta) = -\sin \theta$ $\cos(180^\circ + \theta) = -\cos \theta$ $\tan(180^\circ + \theta) = +\tan \theta$ |
| จตุภาคที่ 4 | $\sin(360^\circ - \theta) = -\sin \theta$ $\cos(360^\circ - \theta) = +\cos \theta$ $\tan(360^\circ - \theta) = -\tan \theta$ $\sin(-\theta) = -\sin \theta$ $\cos(-\theta) = +\cos \theta$ $\tan(-\theta) = -\tan \theta$ |

| | |
|-------------|-------------------------------------------------------------------------------------------------------------------------------------|
| จตุภาคที่ 1 | $\sin(90^\circ - \theta) = \cos \theta$ $\cos(90^\circ - \theta) = \sin \theta$ $\tan(90^\circ - \theta) = \cot \theta$ |
| จตุภาคที่ 2 | $\sin(90^\circ + \theta) = +\cos \theta$ $\cos(90^\circ + \theta) = -\sin \theta$ $\tan(90^\circ + \theta) = -\cot \theta$ |
| จตุภาคที่ 3 | $\sin(270^\circ - \theta) = -\cos \theta$ $\cos(270^\circ - \theta) = -\sin \theta$ $\tan(270^\circ - \theta) = +\cot \theta$ |
| จตุภาคที่ 4 | $\sin(270^\circ + \theta) = -\cos \theta$ $\cos(270^\circ + \theta) = +\sin \theta$ $\tan(270^\circ + \theta) = -\cot \theta$ |

$$\begin{aligned} \text{V} \quad \sin(A+B) &= \sin A \cos B + \cos A \sin B \\ \sin(A-B) &= \sin A \cos B - \cos A \sin B \\ \cos(A+B) &= \cos A \cos B - \sin A \sin B \\ \cos(A-B) &= \cos A \cos B + \sin A \sin B \\ \tan(A+B) &= \frac{\tan A + \tan B}{1 - \tan A \tan B} \end{aligned}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$\begin{aligned} \text{VI} \quad \sin 2A &= 2 \sin A \cos A \\ \cos 2A &= \cos^2 A - \sin^2 A \\ &= 1 - 2 \sin^2 A \\ &= 2 \cos^2 A - 1 \end{aligned}$$

$$1 + \cos 2A = 2 \cos^2 A$$

$$1 - \cos 2A = 2 \sin^2 A$$

$$\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

$$\begin{aligned} \text{VII} \quad \sin 3A &= 3 \sin A - 4 \sin^3 A \\ \cos 3A &= 4 \cos^3 A - 3 \cos A \\ \tan 3A &= \frac{3 \tan A - \tan^3 A}{1 - 3 \tan^2 A} \end{aligned}$$

$$\text{VIII} \quad \text{ถ้ } t = \tan \frac{\theta}{2} \text{ แล้ว}$$

$$\sin \theta = \frac{2t}{1+t^2}$$

$$\cos \theta = \frac{1-t^2}{1+t^2}$$

$$\tan \theta = \frac{2t}{1-t^2}$$

$$\begin{aligned} \text{IX} \quad 2 \sin A \cos B &= \sin(A+B) + \sin(A-B) \\ 2 \cos A \sin B &= \sin(A+B) - \sin(A-B) \\ 2 \cos A \cos B &= \cos(A+B) + \cos(A-B) \\ 2 \sin A \sin B &= \cos(A-B) - \cos(A+B) \end{aligned}$$

X

$$\sin C + \sin D = 2 \sin \frac{C+D}{2} \cos \frac{C-D}{2}$$

$$\sin C - \sin D = 2 \cos \frac{C+D}{2} \sin \frac{C-D}{2}$$

$$\cos C + \cos D = 2 \cos \frac{C+D}{2} \cos \frac{C-D}{2}$$

$$\cos C - \cos D = 2 \sin \frac{C+D}{2} \sin \frac{D-C}{2}$$

XI

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$b^2 = c^2 + a^2 - 2ca \cos B$$

$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$\text{W. A. } \Delta ABC = \frac{1}{2} ab \sin C$$

$$= \frac{1}{2} bc \sin A$$

$$= \frac{1}{2} ca \sin B$$

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$\text{W. A. } s = \frac{1}{2} (a+b+c)$$

